



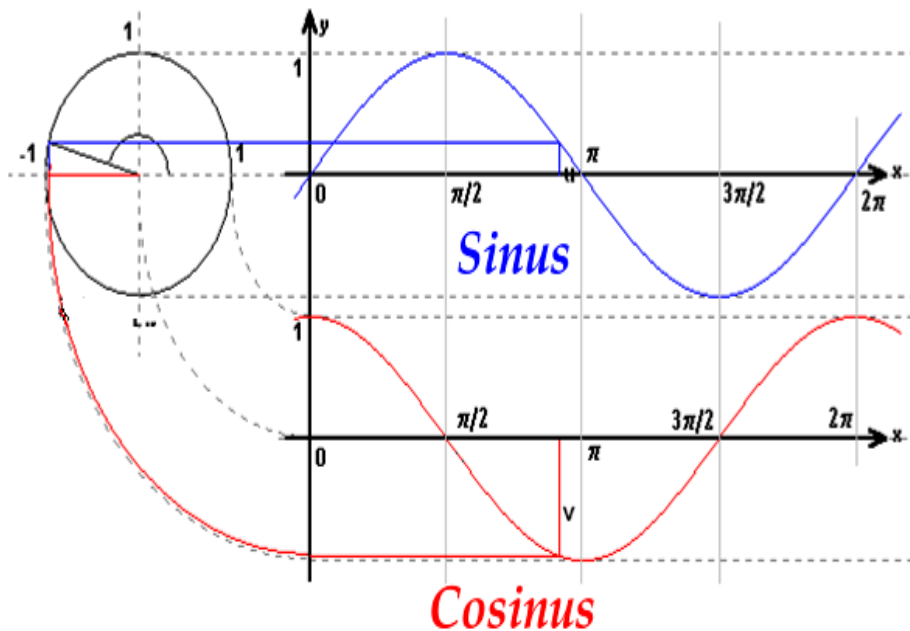
Examples of good practice

Mathematics

Teacher Adina Vasilica

Trigonometric functions **sin** & **cos**

- **General goals :**
- - forming skills and abilities;
- - achieving and thoroughgoing study of new knowledge;
- **Operational goals :**
- - the pupils should be able to recognize different values in radians on the trigonometric circle;
- -- the pupils should use correctly the dynamic elements of the lesson;
- - the pupils should be able to establish correctly the differences between sin and cos
- **Didactic strategies :**
- - didactic methods and procedures: communication methods, practical activities methods, verifying and evaluating the results methods
- - frontal methods of organizing the lesson



LESSON PLANNING: TEACHER'S ACTIVITIES

1. Preparing the pupils for the lesson (2 minutes)

2. Reviewing the useful knowledge and preparing the new lesson (7 minutes)

- momentul **m1** : o scurtă amintire a funcției de trecere de la dreapta reală la cercul trigonometric și a proprietăților acesteia ; activitatea desfășurată de elevi reprezintă studiul reprezentării grafice pe cercul trigonometric a valorilor uzual întâlnite : valorile putând fi selectate de către elevi.

3. Teaching the new knowledge (20 minutes)

- momentul **m2** : definirea funcțiilor sinus și cosinus, reprezentarea acestora pe cercul trigonometric ; exemplu de aflare a funcțiilor uzuale.
- momentul **m3** : prezentarea tabelului de valori al funcțiilor sin și cos ; elevii studiază graficul funcției sinus pe intervalul, grafic ce face corespondența între cercul trigonometric și dreapta reală.
- momentul **m4** : proprietăți fundamentale ale funcțiilor : sin și cos ; activitatea desfășurată de elevi reprezintă validarea unei soluții trigonometrice de forma :
 - Este studiată reducerea la primul cadran.
- momentul **m5** : reprezentarea grafică a funcțiilor sinus și cosinus, studiul semnului acestora pentru cele IV cadrane.

4. Fixing and strenghtening the knowledge achieved (10 minutes)

- momentul **m6** : profesorul discută reprezentările grafice ale funcțiilor în același sistem de axe.

5. Test (10 minutes)

- fiecare elev va răspunde la 5 întrebări propuse ce vor constitui pentru profesor o metodă de verificare / evaluare activă și dinamică a rezultatelor .

6. Homework (1 minute)

SIN



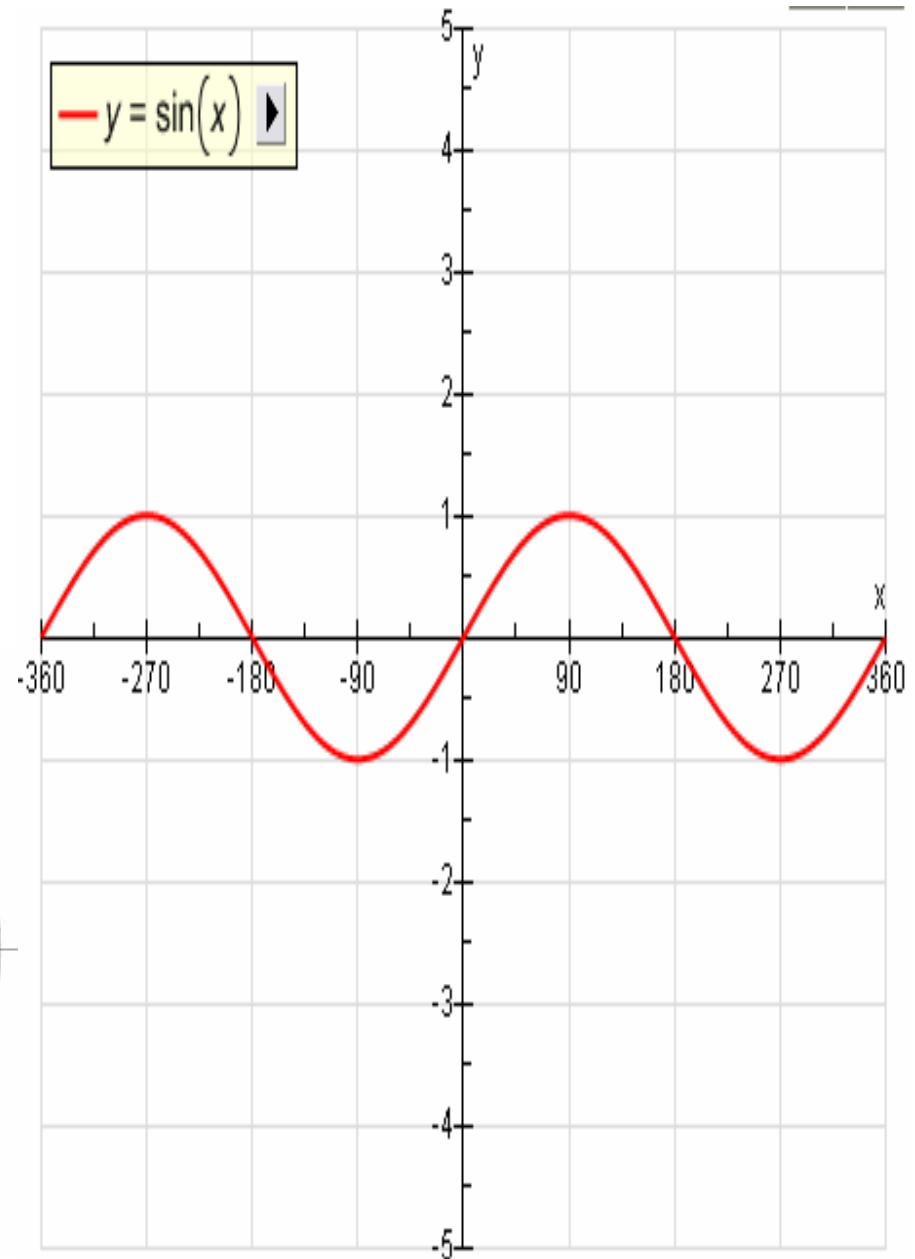
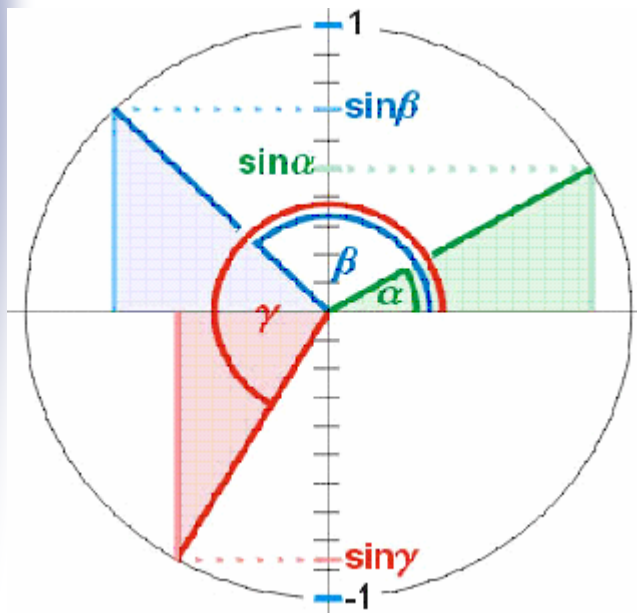
Domeniu f: $-\infty < x < \infty$

Codomeniu f: $-1 \leq y \leq 1$

Perioada: 2π

$$\sin(x + 2k\pi) = \sin x$$

$\sin(-x) = -\sin x$ **–funcție impară**



COS



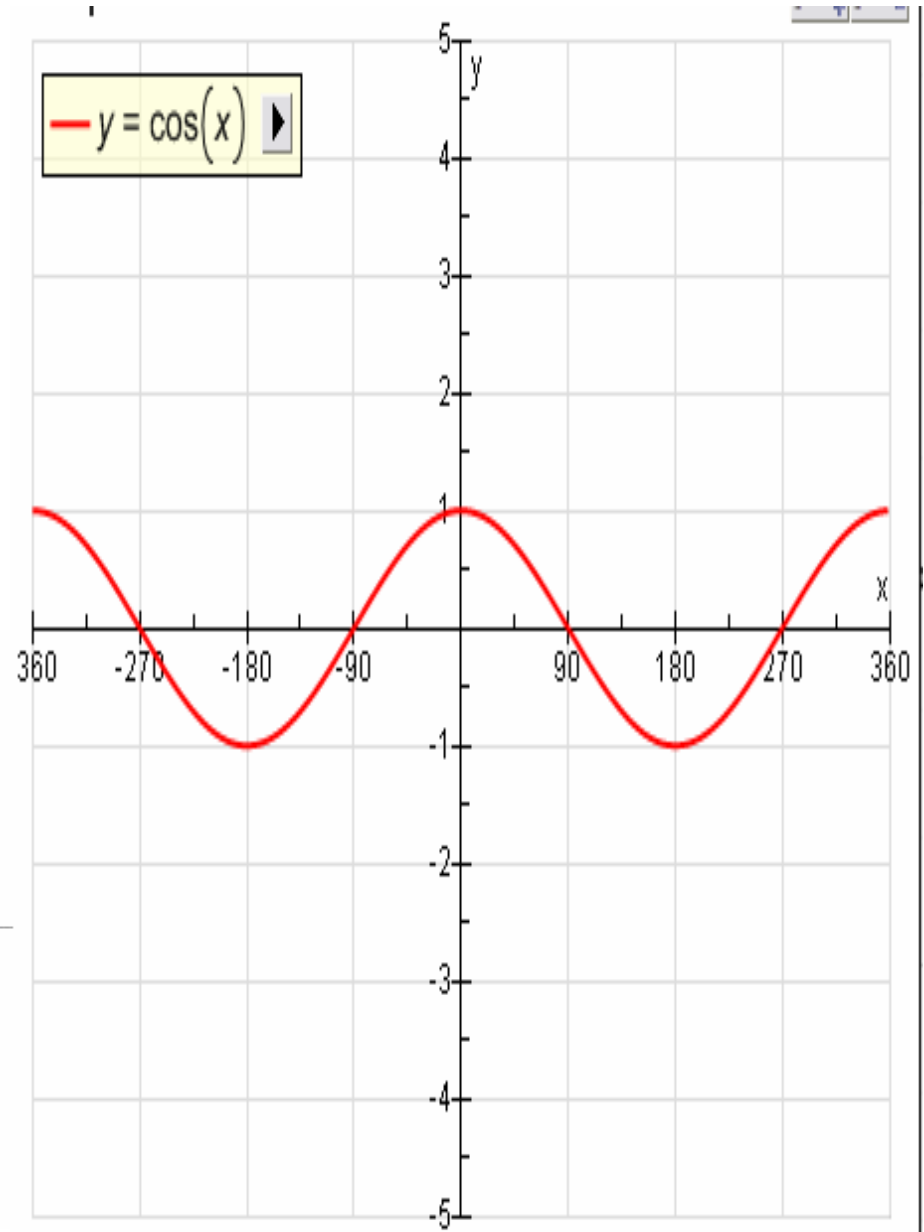
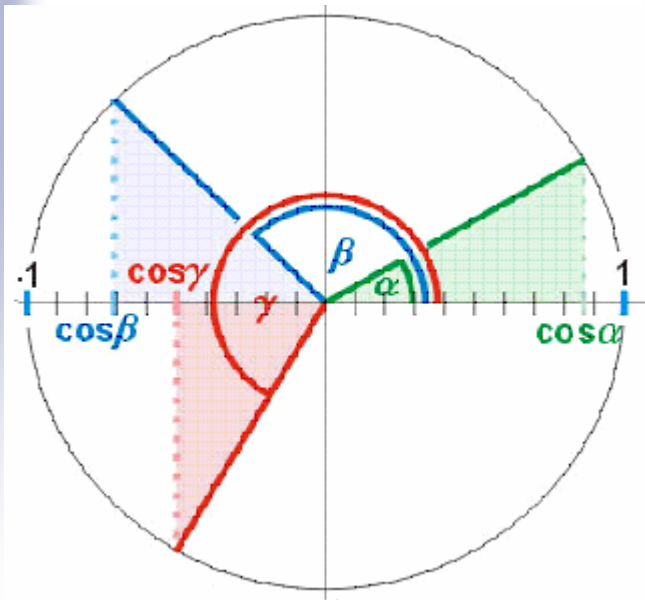
Domeniu f: $-\infty < x < \infty$

Codomeniu f: $-1 \leq y \leq 1$

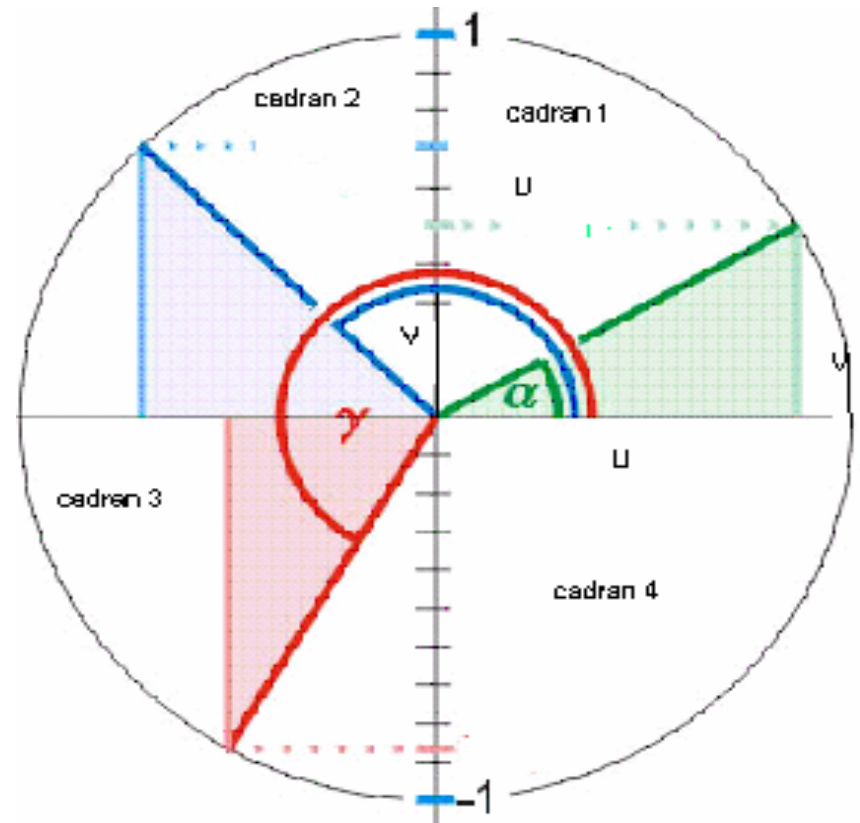
Perioada: 2π

$$\cos(x + 2k\pi) = \cos x$$

$\cos(-x) = \cos x$ – funcție pară

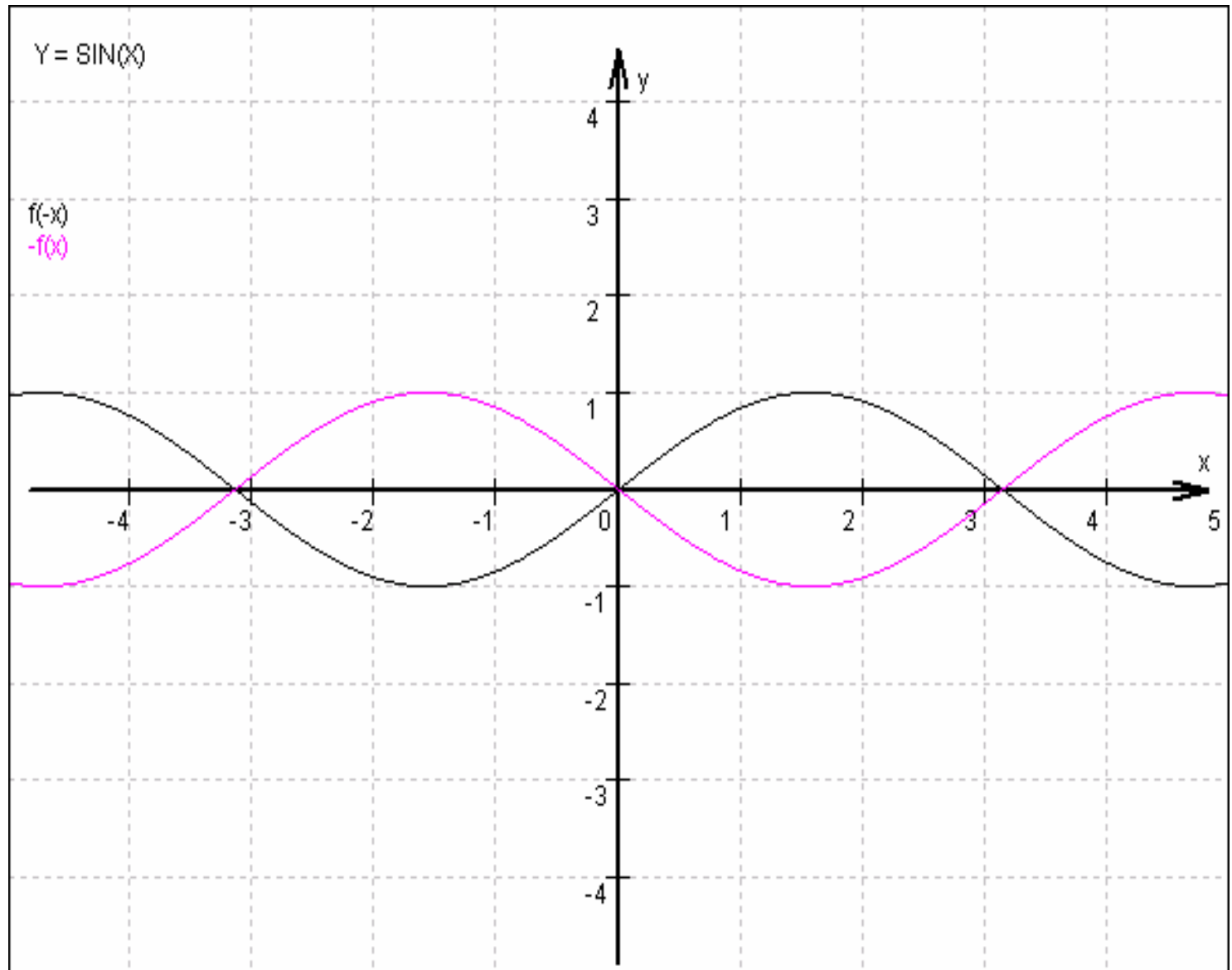


- $y = \sin \alpha = v$
- $y = \cos \alpha = u$

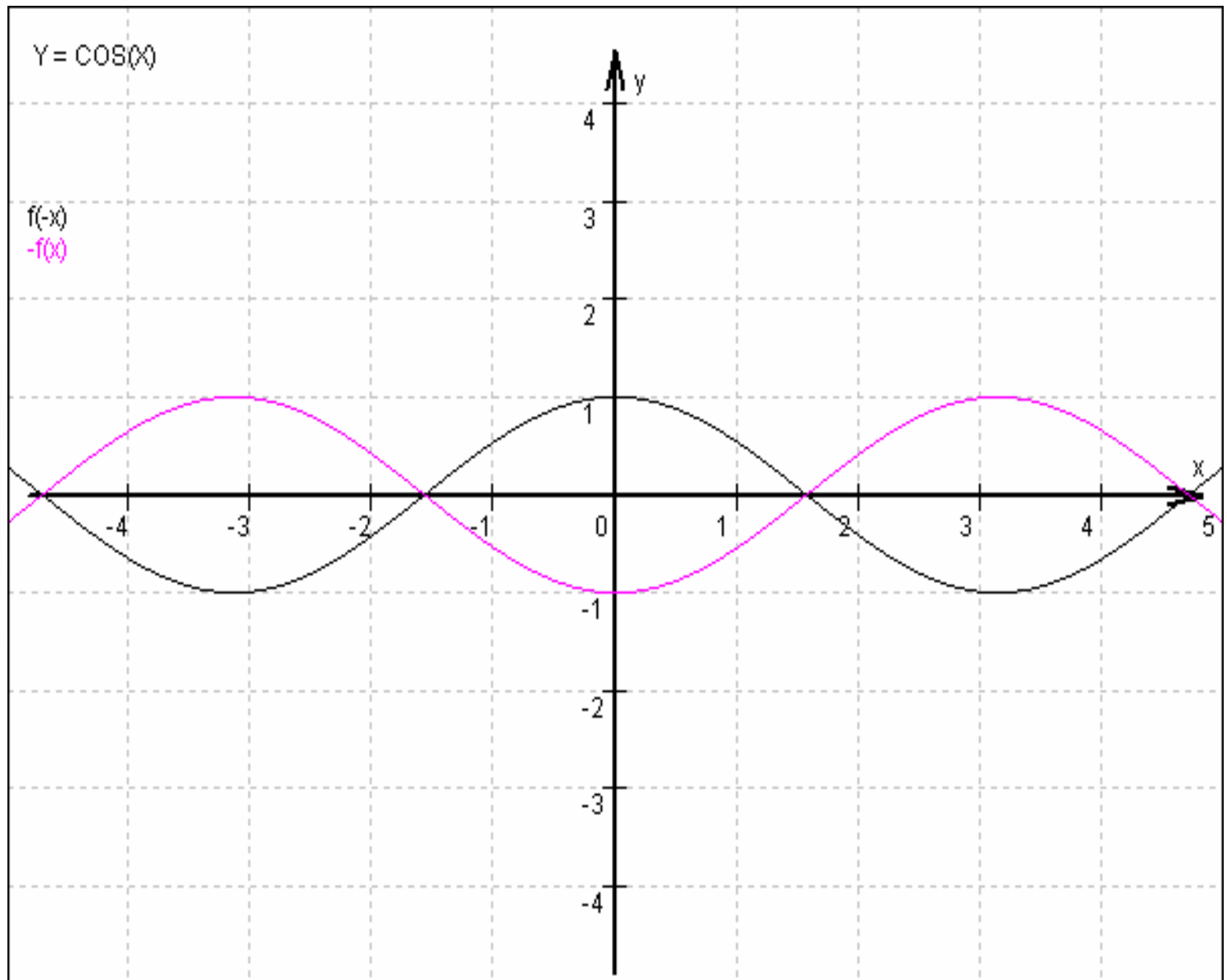


Cadran	1	2	3	4
	x	$\pi - x$	$\pi + x$	$2\pi - x$
sinus	$\sin x$	$\sin x$	$-\sin x$	$-\sin x$
cosinus	$\cos x$	$-\cos x$	$-\cos x$	$\cos x$

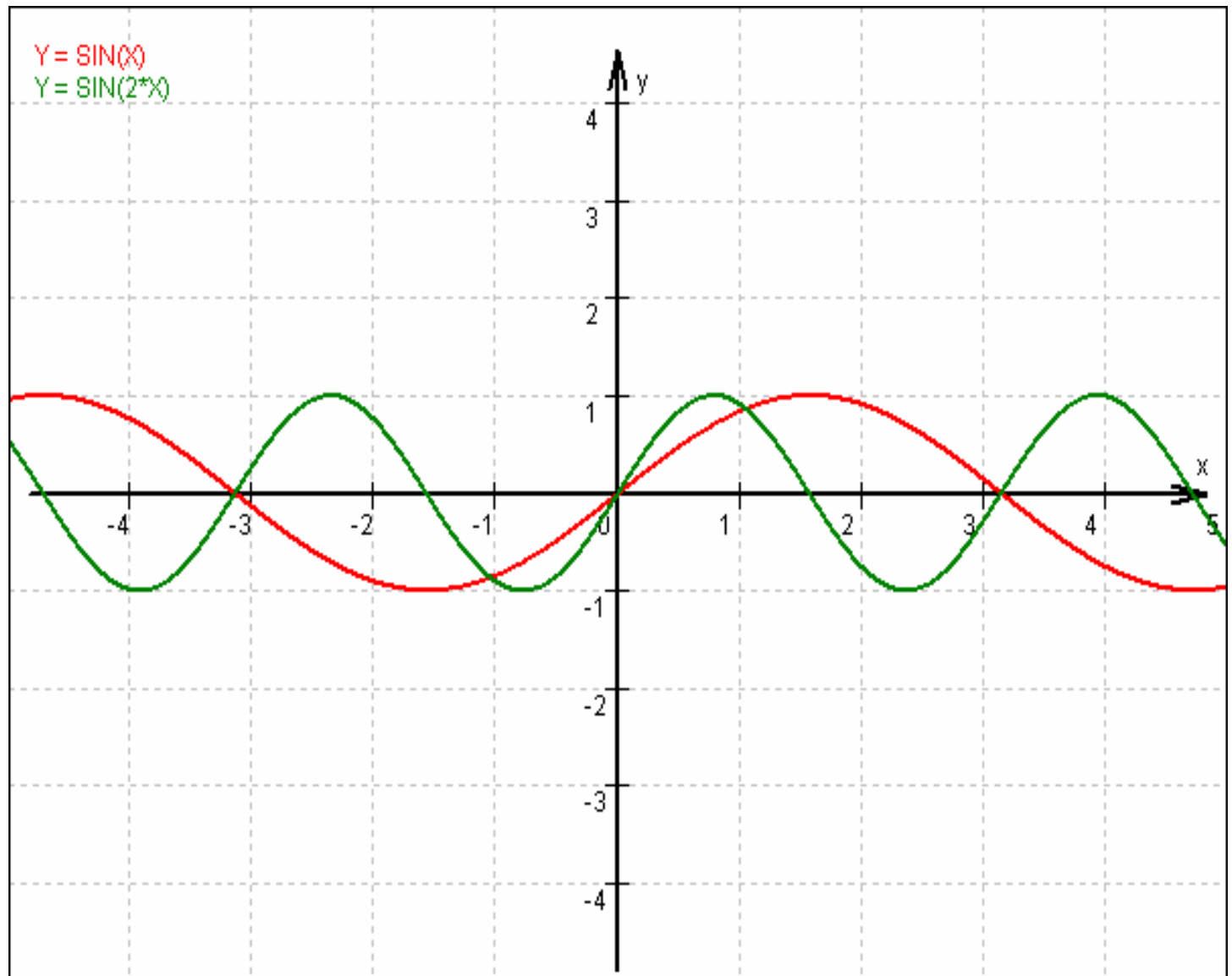
Y = f(x) = sin(x) ; f(-x) = sin(-x) = -sin(x) = -f(x)



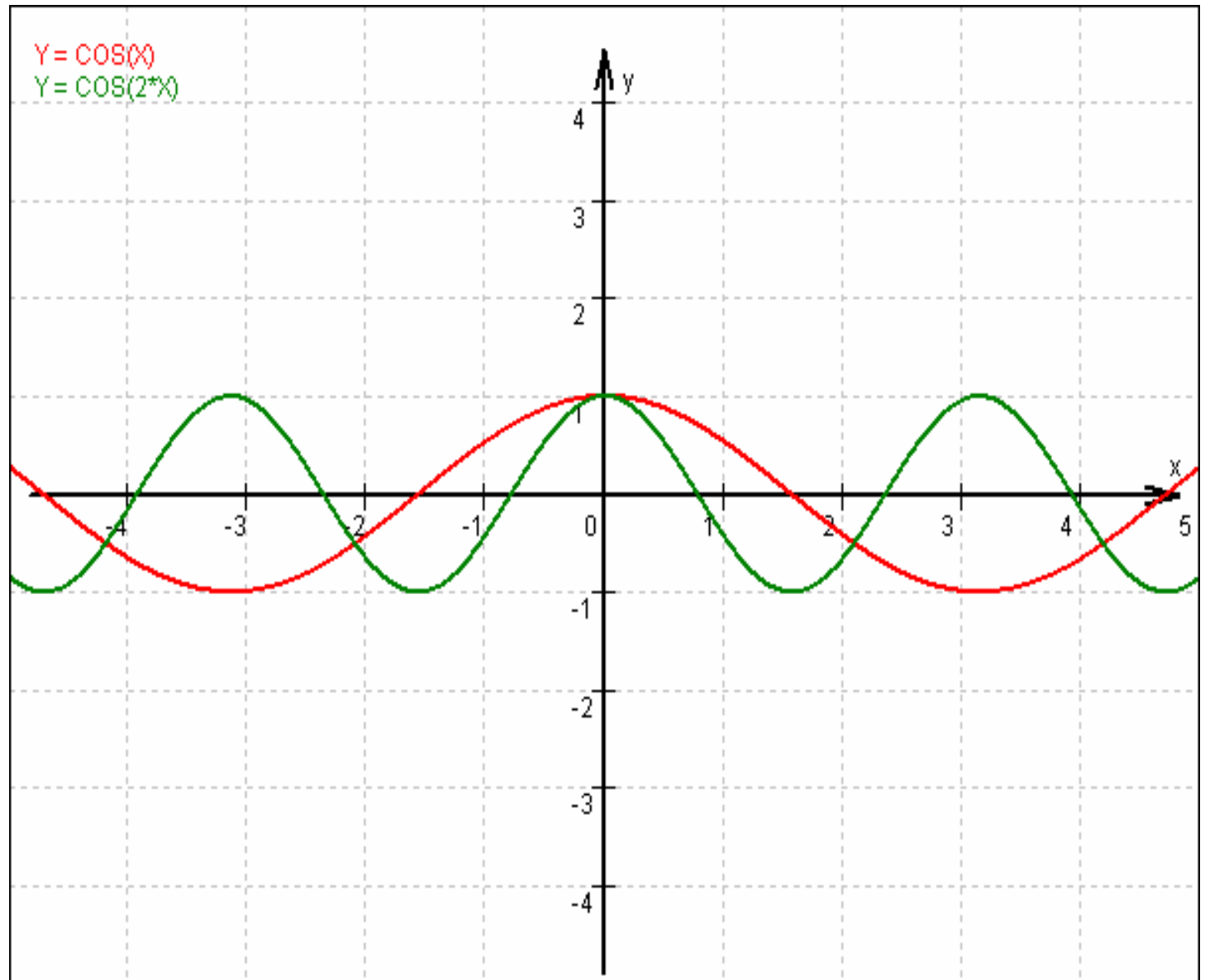
$Y = f(x) = \cos(x); \quad f(-x) = \cos(-x) = \cos(x); \quad -f(x) = -\cos(x)$



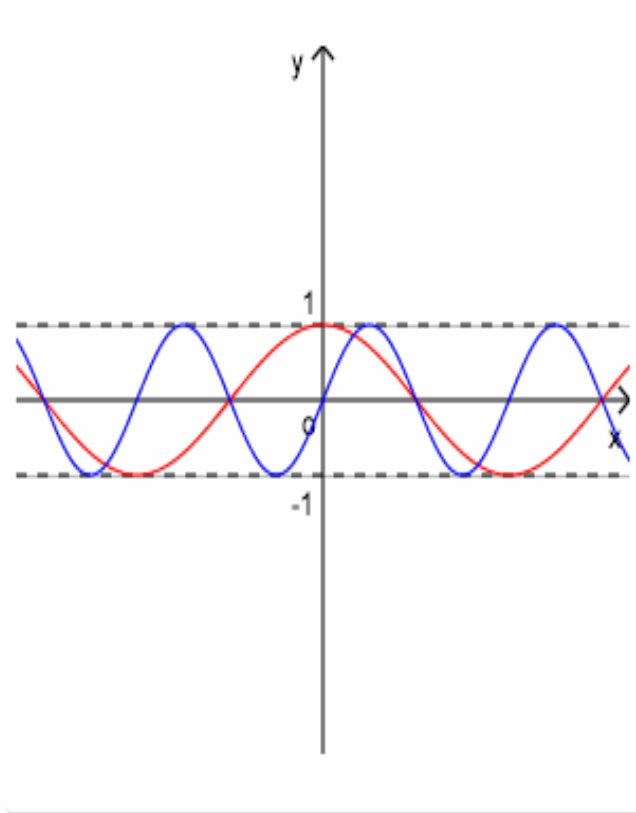
$f(x) = \sin x$; $g(x) = \sin(2x)$



$f(x)=\cos x$; $g(x)=\cos (2x)$



AEL exercises:

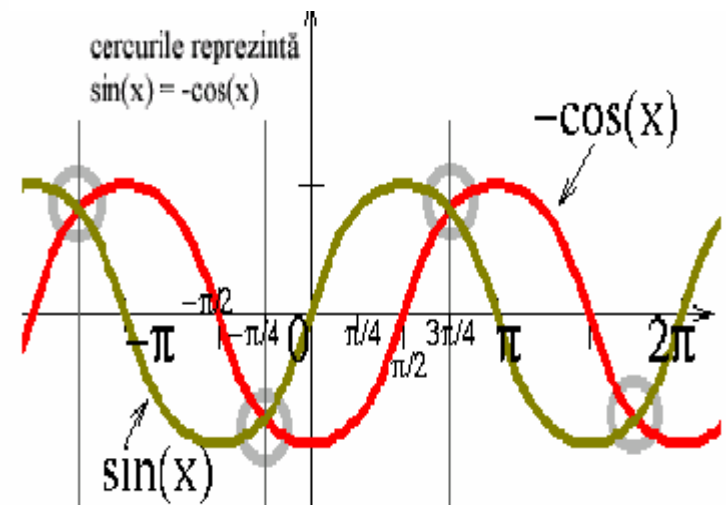


$f(x) = \sin(2x + 0\pi)$

$f(x) = \cos(1x + 0\pi)$

Ezercițiu :

Studiați figurile următoare discutându-le pe fiecare detaliat :



Applications with definite integral in Plan Geometry

Ariile unor suprafețe plane

- $f:[a;b] \rightarrow \mathbb{R}$ - funcție continuă, $f(x) \geq 0$ iar $\Gamma f = \{(x,y) | a \leq x \leq b, 0 \leq y \leq f(x)\}$ este subgraficul lui f , atunci Γf are aria:

$$\text{aria}(\Gamma f) = \int_a^b f(x) dx$$

1. Dacă $f(x) \geq 0$ atunci

$$\text{aria}(\Gamma f) \geq 0$$

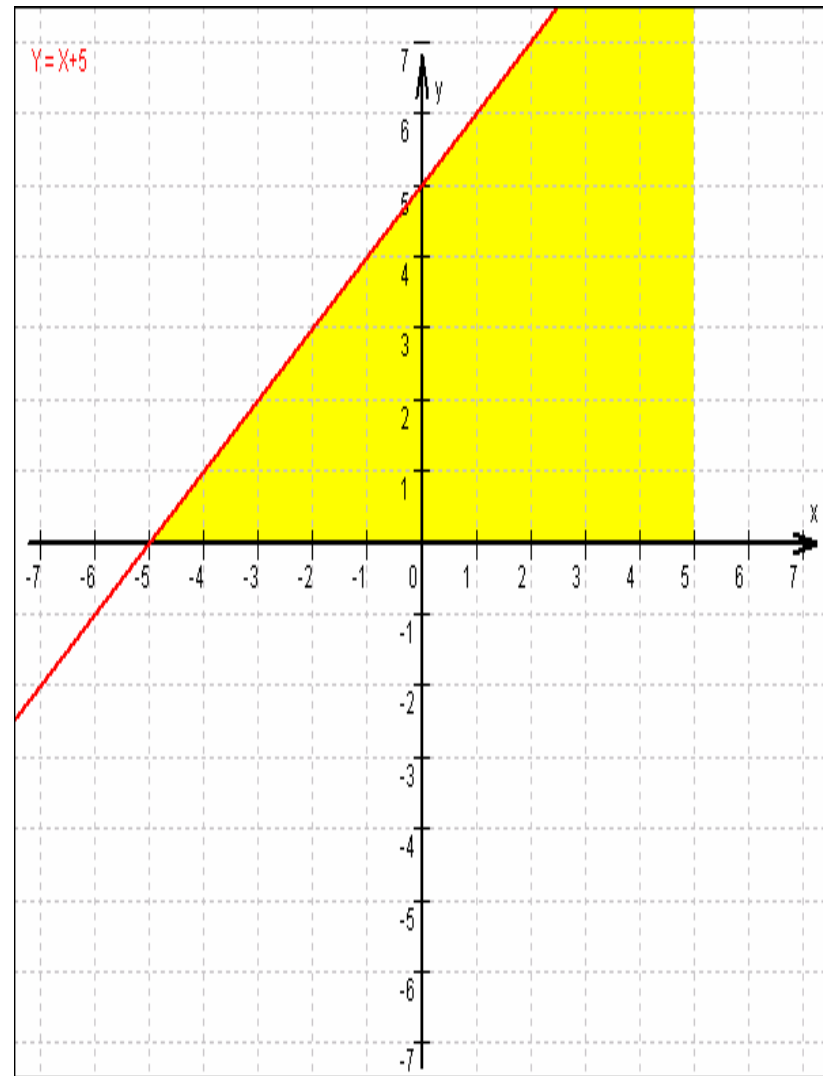
2. Dacă $f(x) \leq 0$ atunci graficul lui f este sub axa Ox

și

$$\text{aria}(\Gamma f) = - \int_a^b f(x) dx$$

3. Dacă $f, g:[a;b] \rightarrow \mathbb{R}$ -funcții continue, $f(x) \leq g(x)$, $(\forall) x \in [a;b]$ atunci

$$\text{aria}(\Gamma f) = \int_a^b [g(x) - f(x)] dx$$



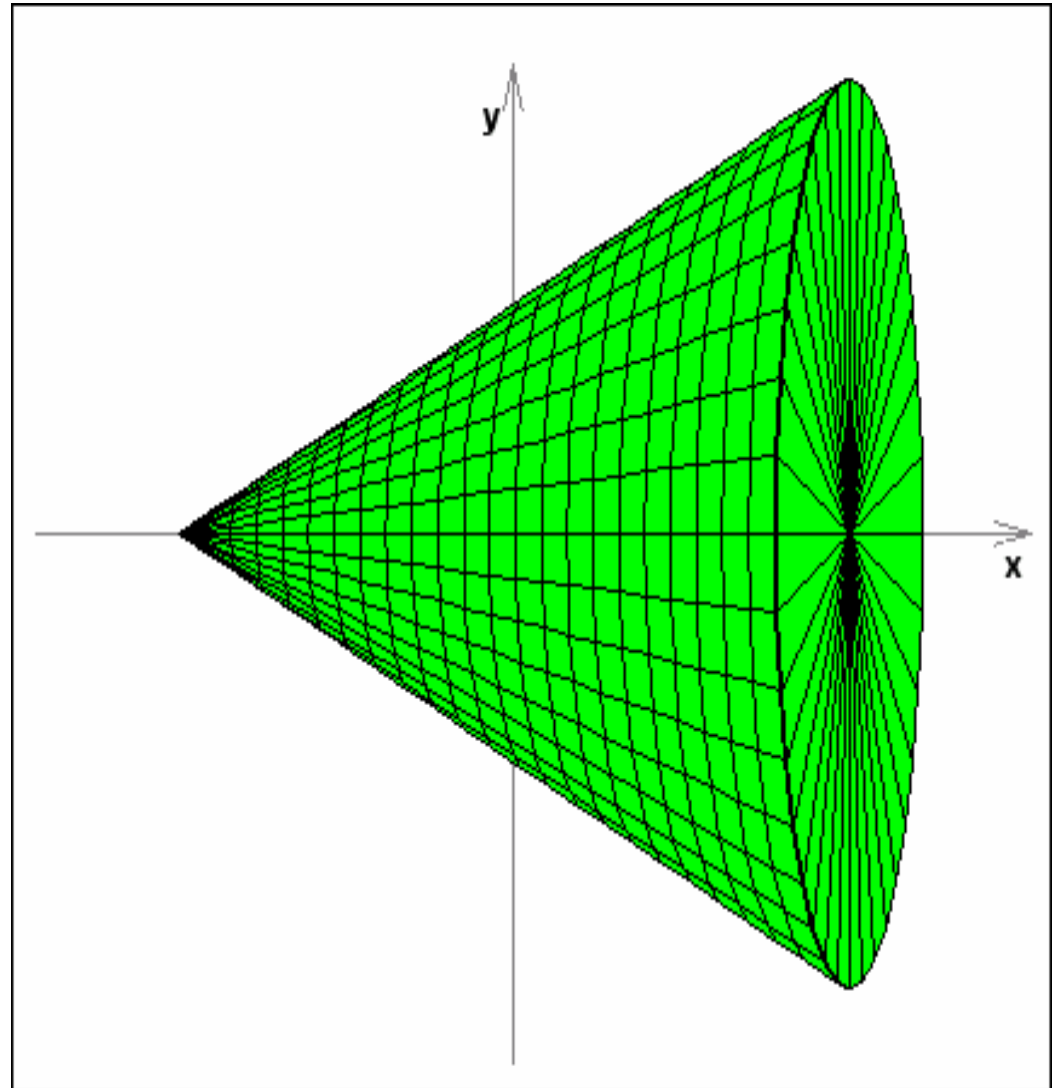
Ex: $f(x) = x + 5$; $\text{aria}(\Gamma f) = 50$

Applications with definite integral in Space Geometry

Volumele corpurilor de rotație

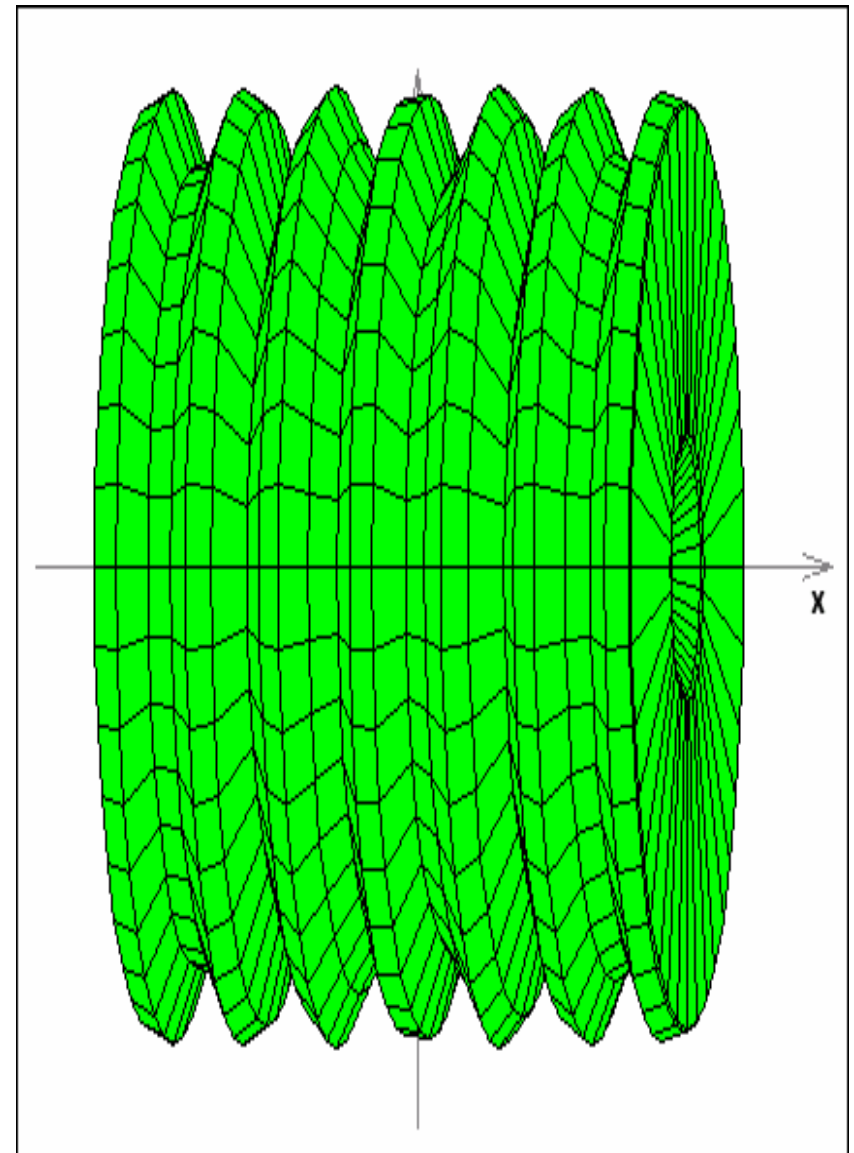
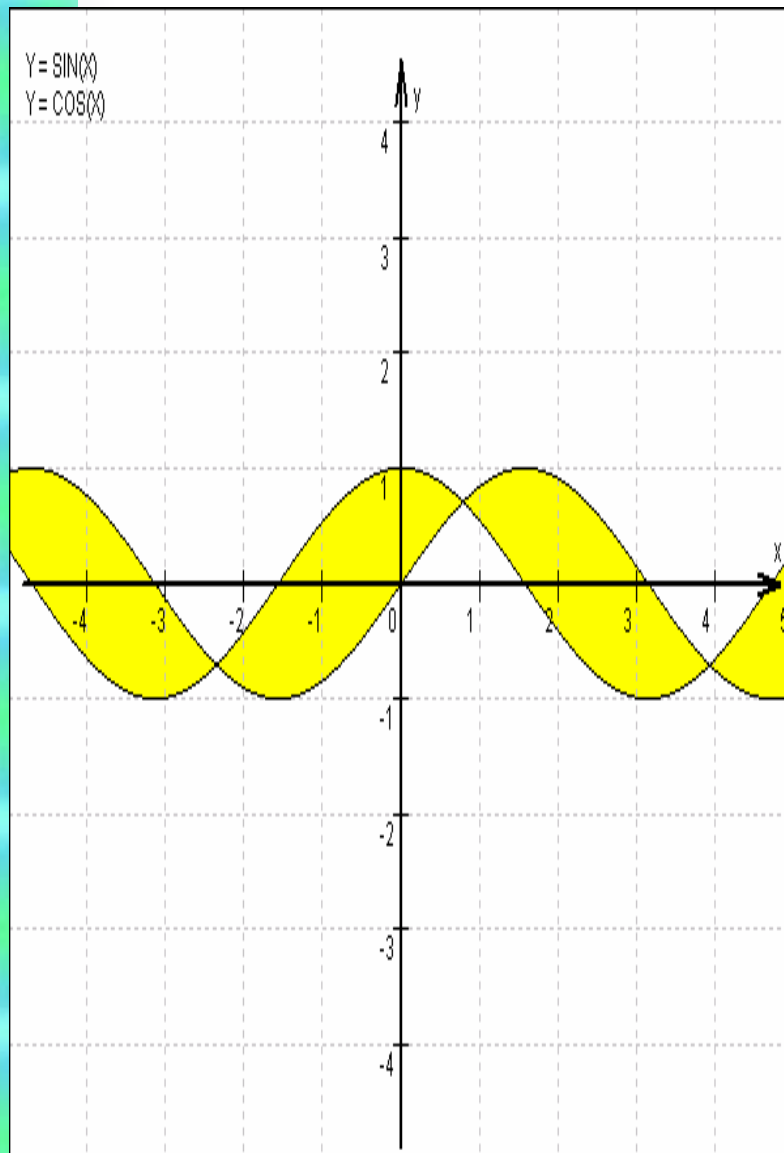
- $f:[a;b] \rightarrow [0;\infty)$ -funcție continua atunci corpul de rotație determinat de f are volumul

$$V(Cf) = \pi \int_a^b f^2(x) dx$$

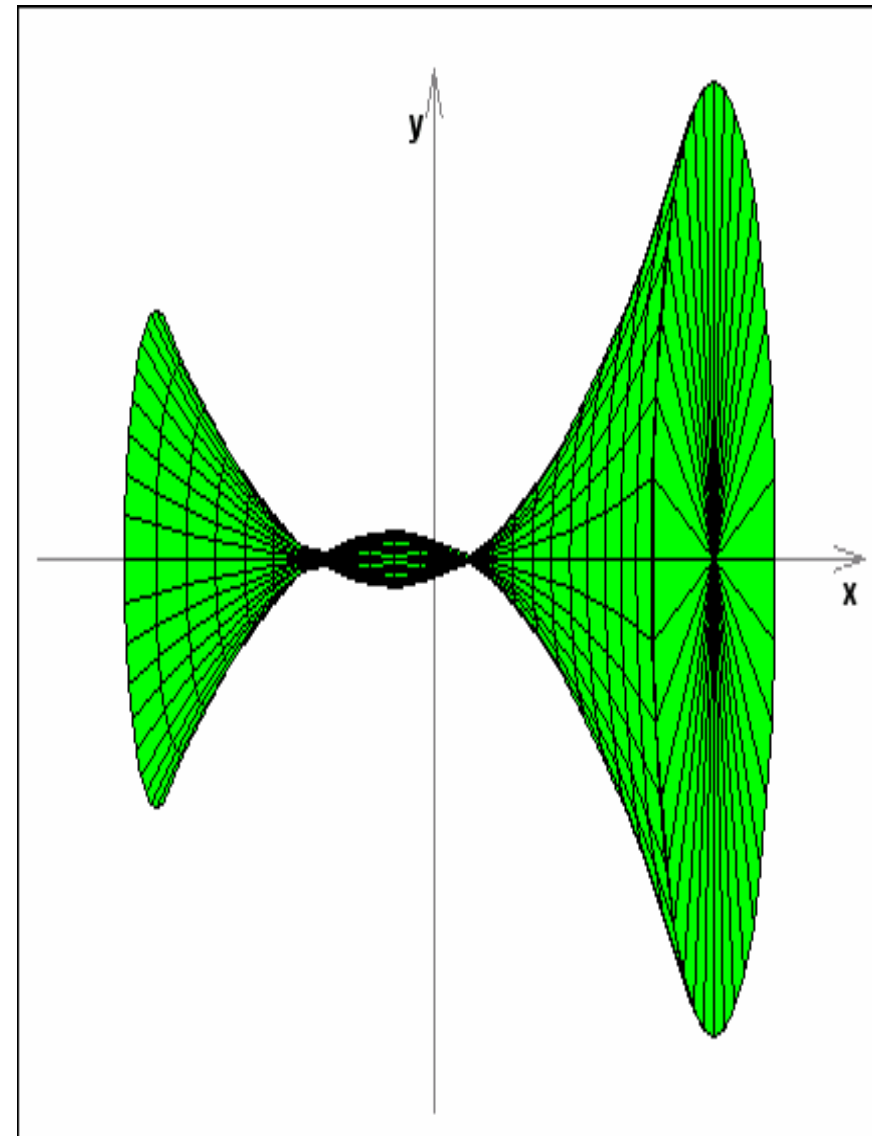
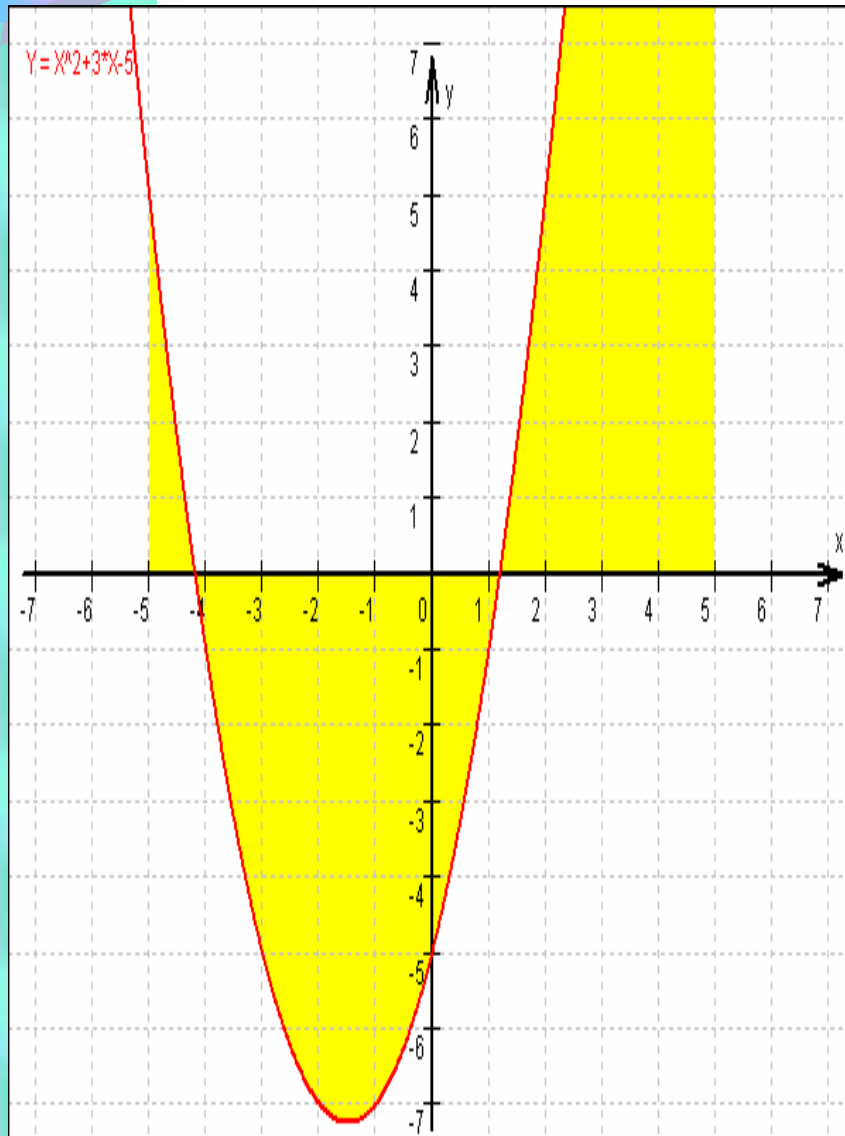


Ex: $f(x)=x+5$; $V(Cf)=(1000/3)\pi$

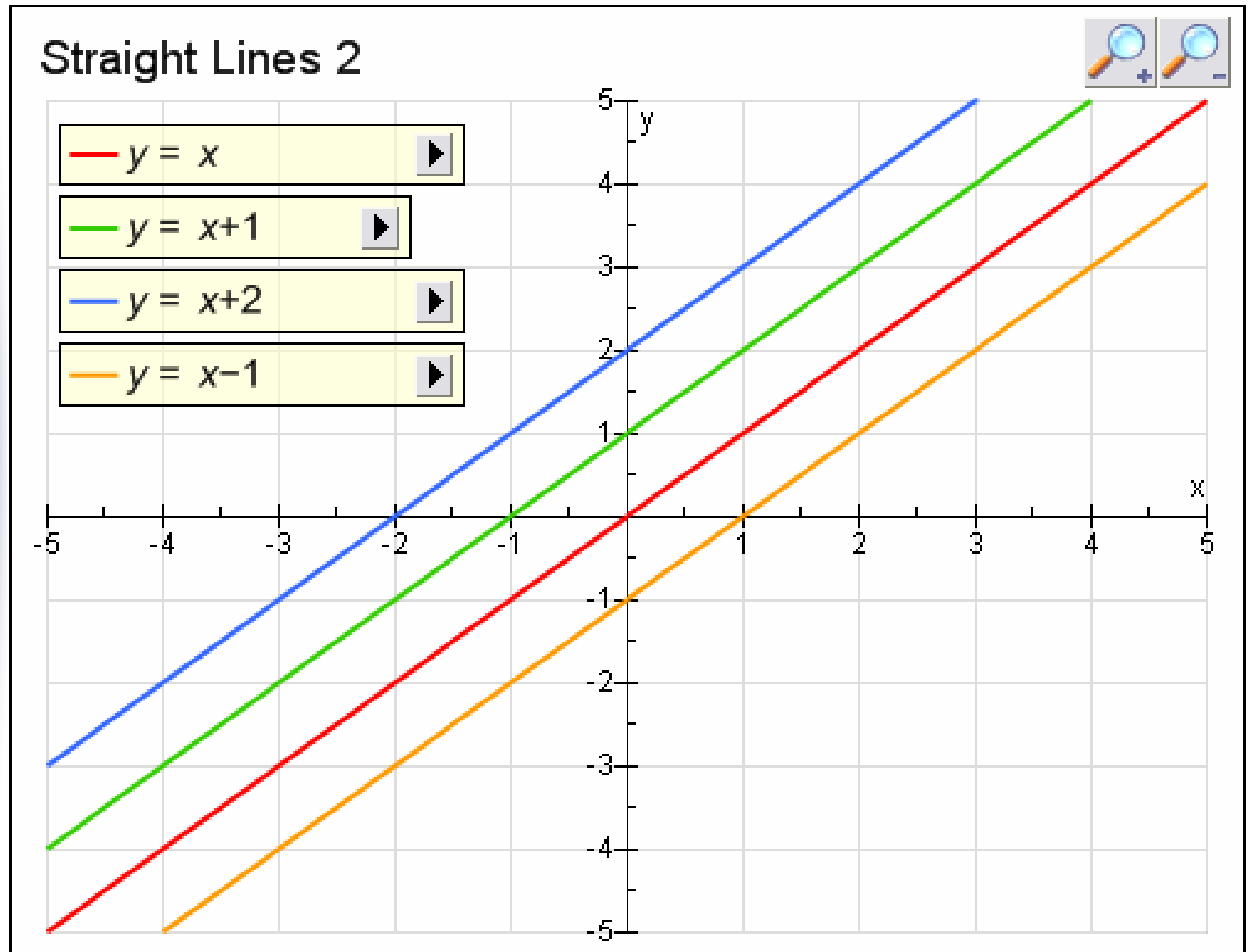
Ex: $f(x) = \sin(x)$, $g(x) = \cos(x)$



Ex: $f(x)=x^2+3x-5$

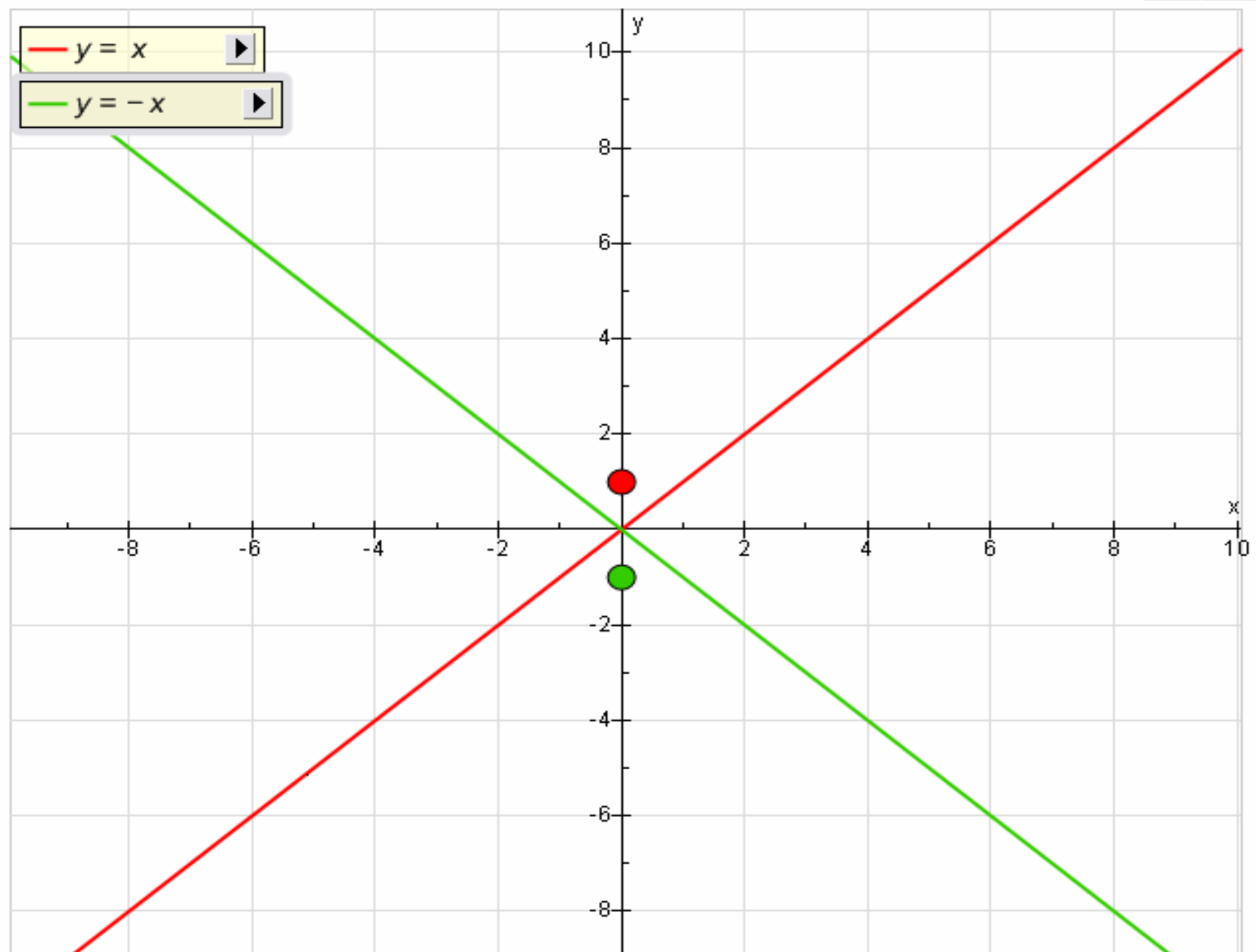


Crocodile Mathematics

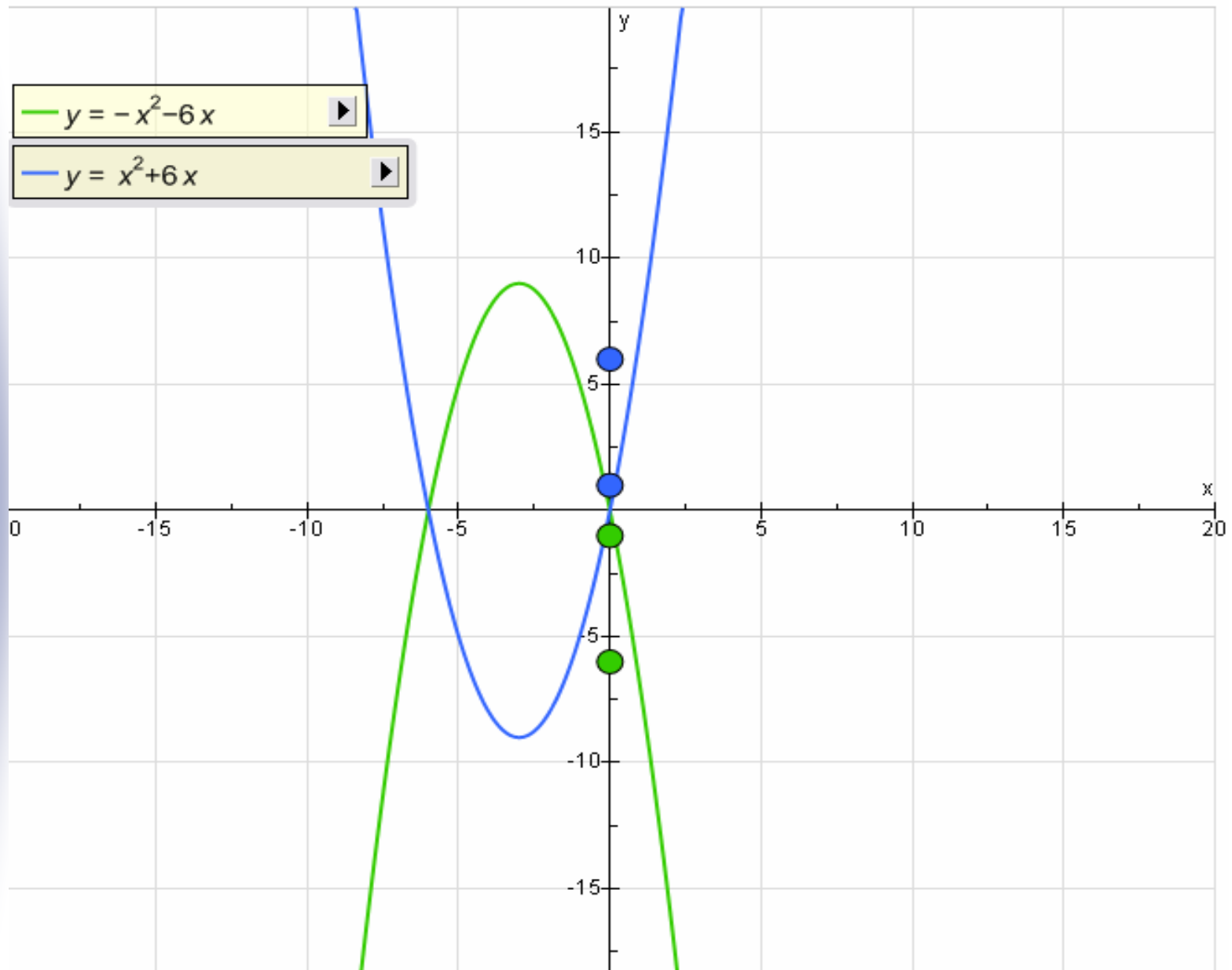


Crocodile Mathematics

Graph 1



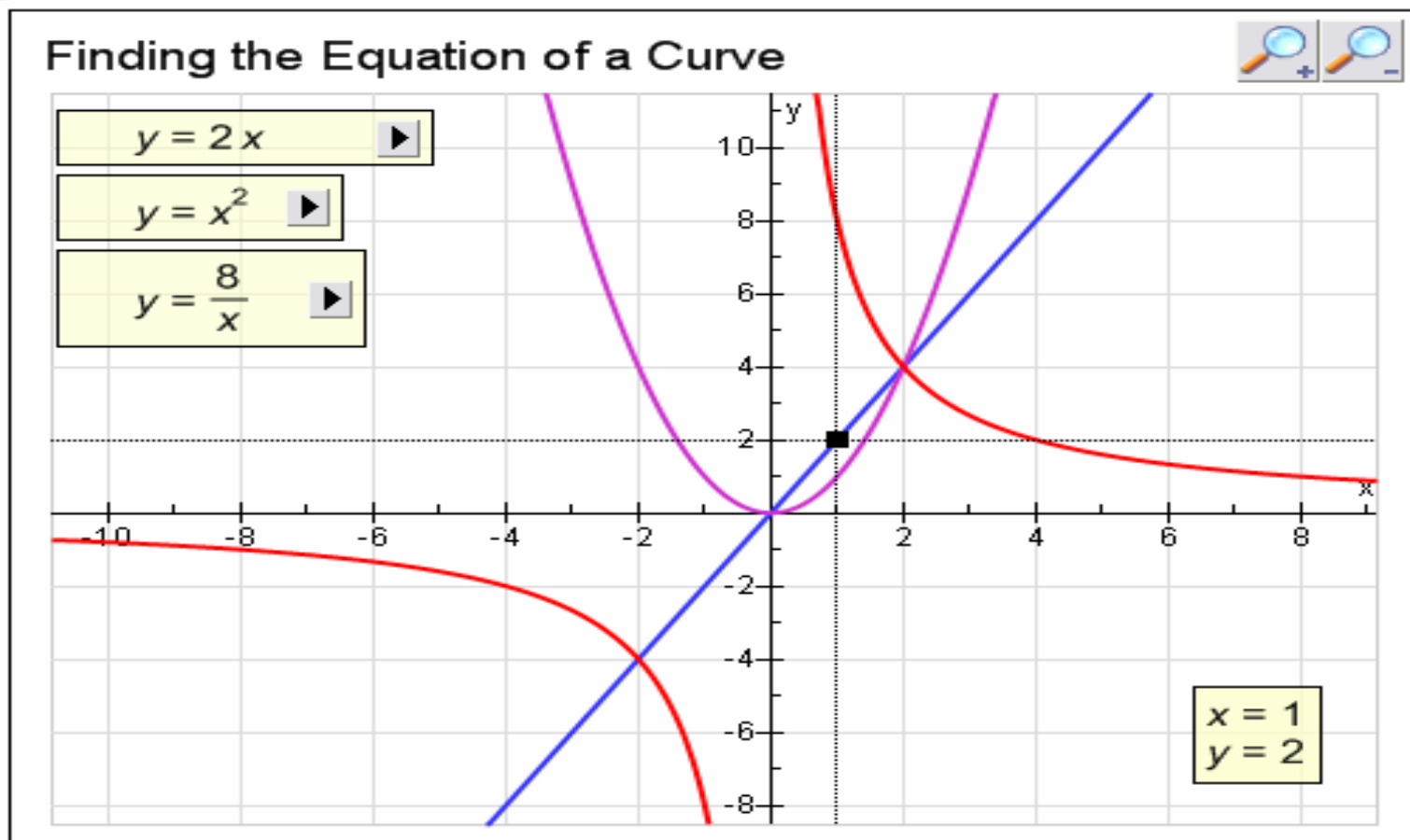
Crocodile Mathematics



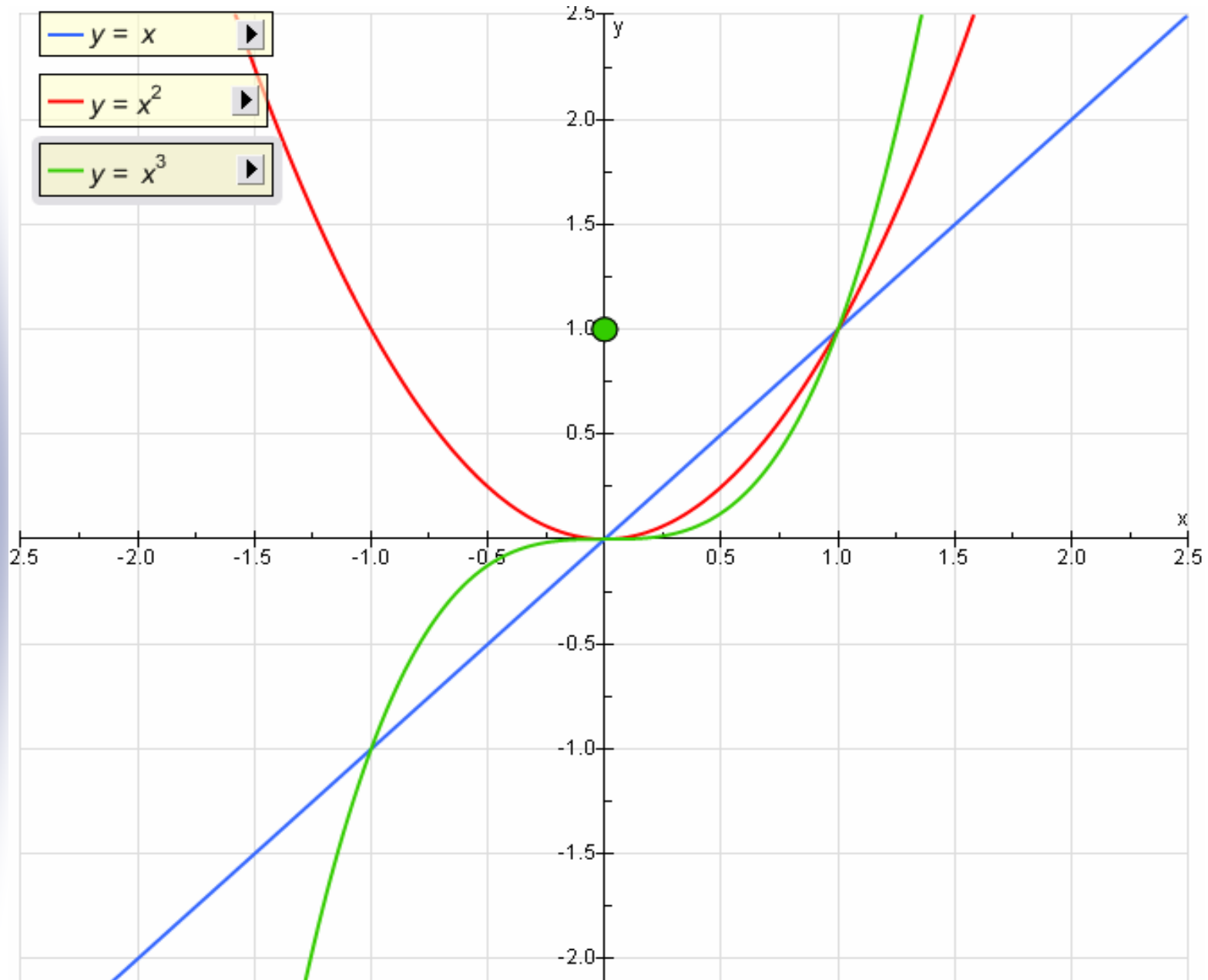
Crocodile Mathematics

Finding the Equation of a Curve

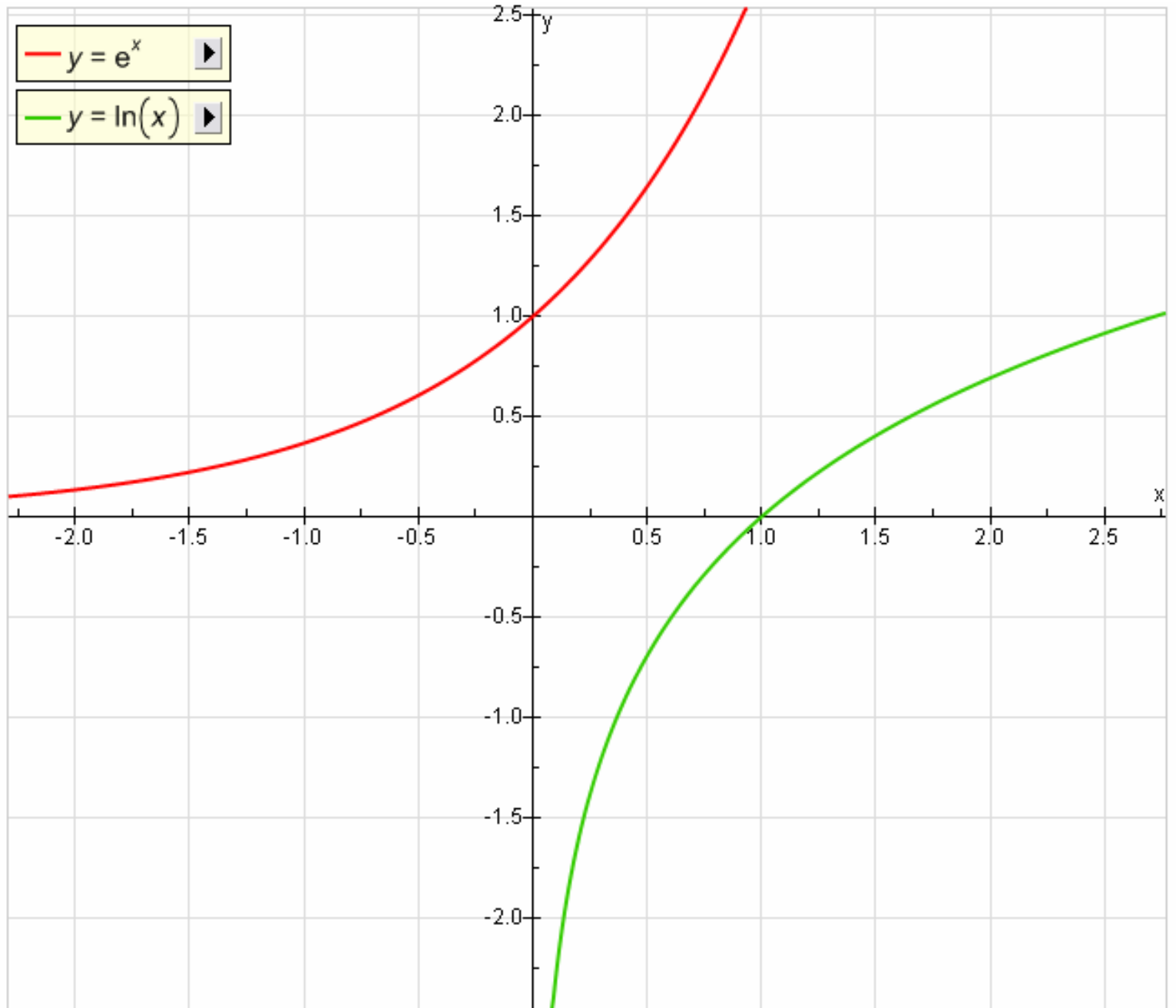
For each curve move the trace point through x values of 1, 2, 3, 4 etc., making note of the x and y values at each point. From this work out which equation relates to which curve.



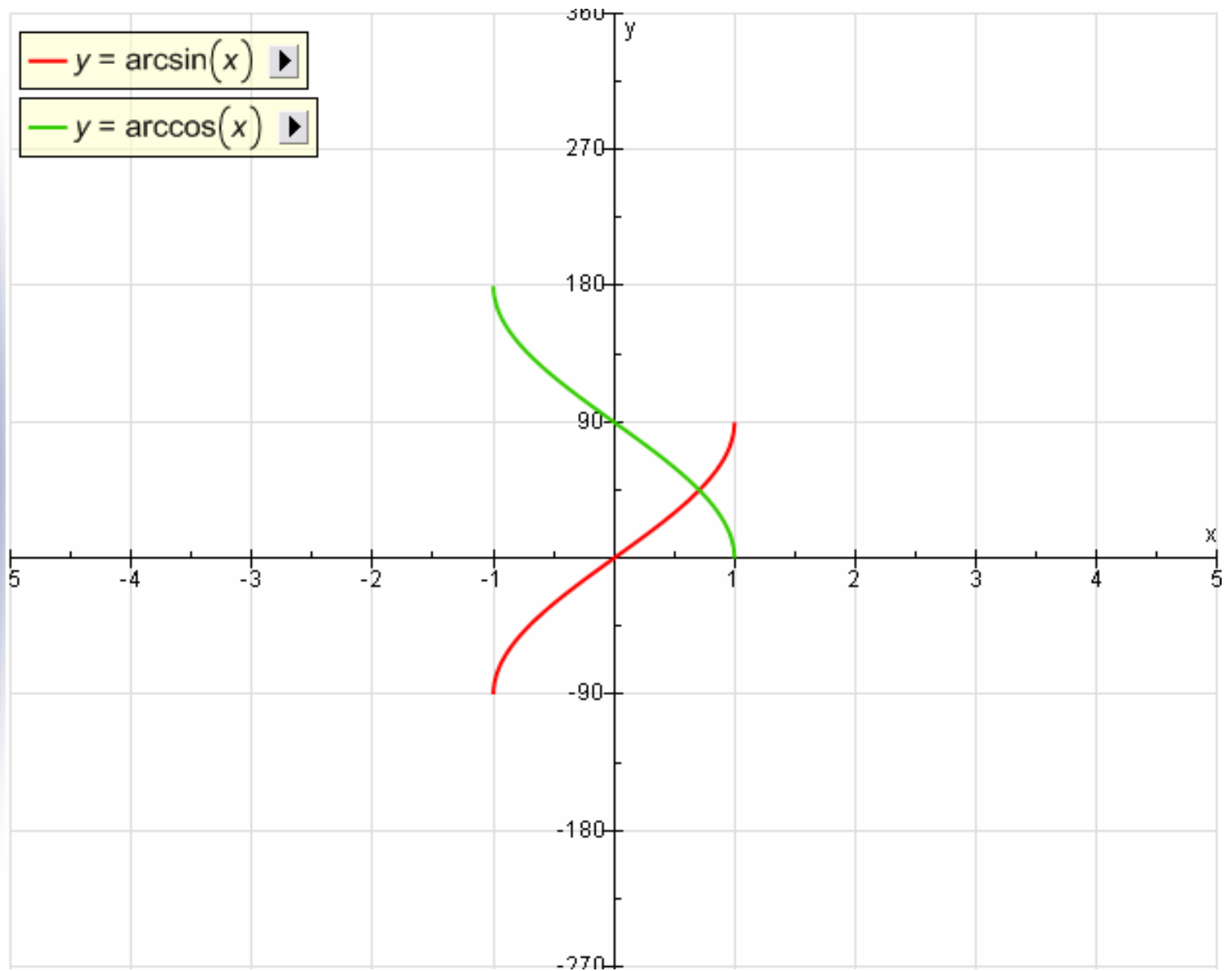
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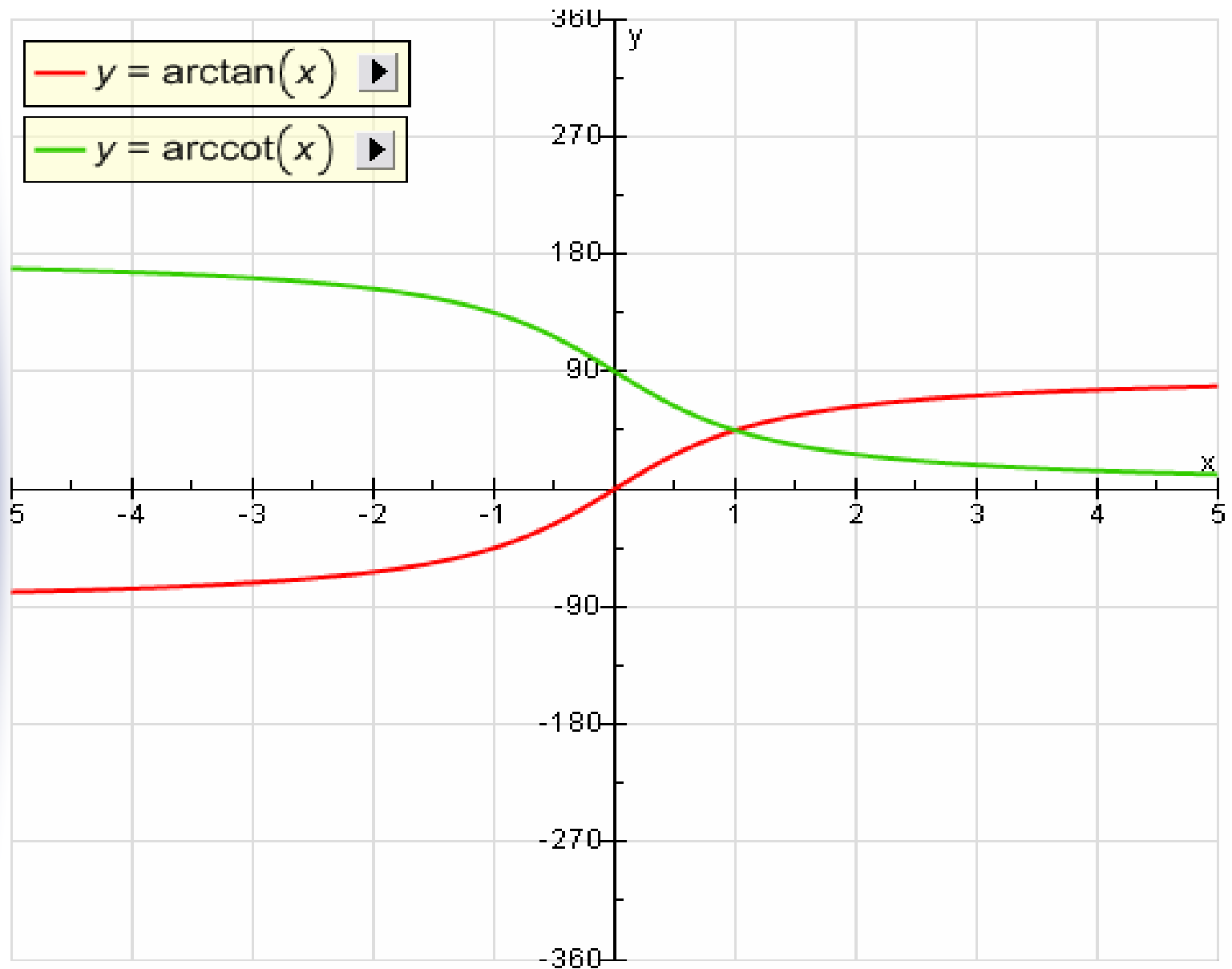
Crocodile Mathematics



Crocodile Mathematics



Crocodile Mathematics

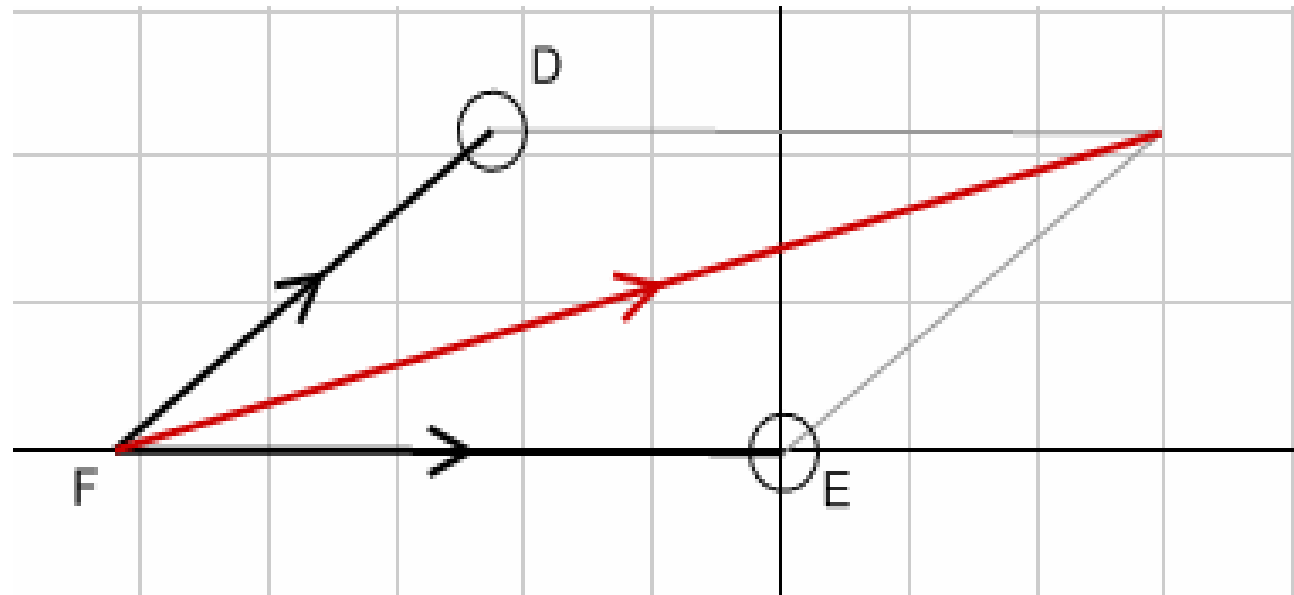


Crocodile Mathematics

Adding Vectors With Parallelograms

One way of adding vectors is shown below:

- draw the two vectors from the same point (FD and FE)
- draw parallel lines to complete the parallelogram
- the resultant is the vector from the starting point to the opposite corner of the parallelogram.

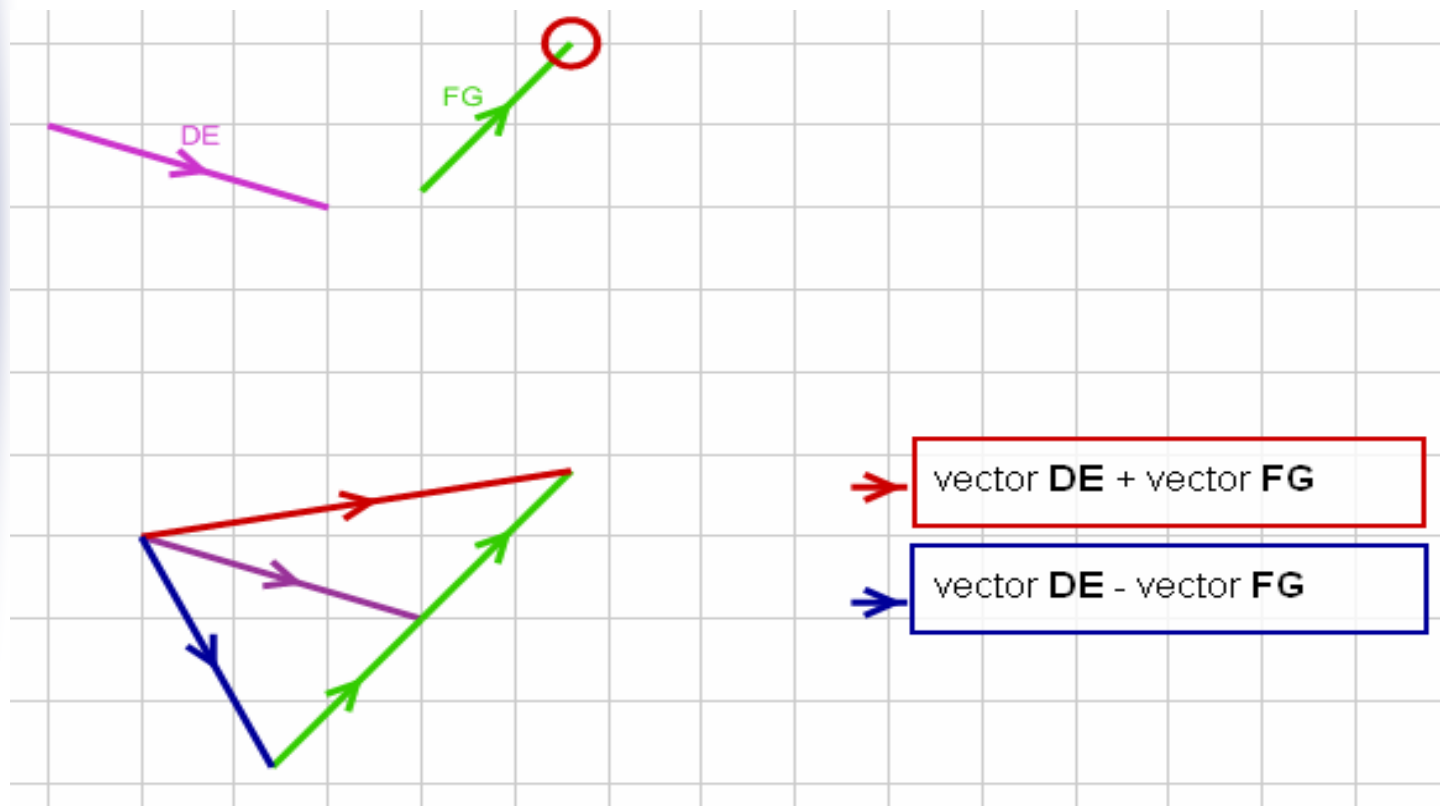


Crocodile Mathematics

Adding and Subtracting Vectors

You can move the vector FG below by dragging the red circle. Below them a diagram shows the result of adding vector DE to vector FG , and the result of subtracting vector FG from vector DE .

Subtracting vector FG from vector DE is the same as adding the inverse of vector FG to vector DE .

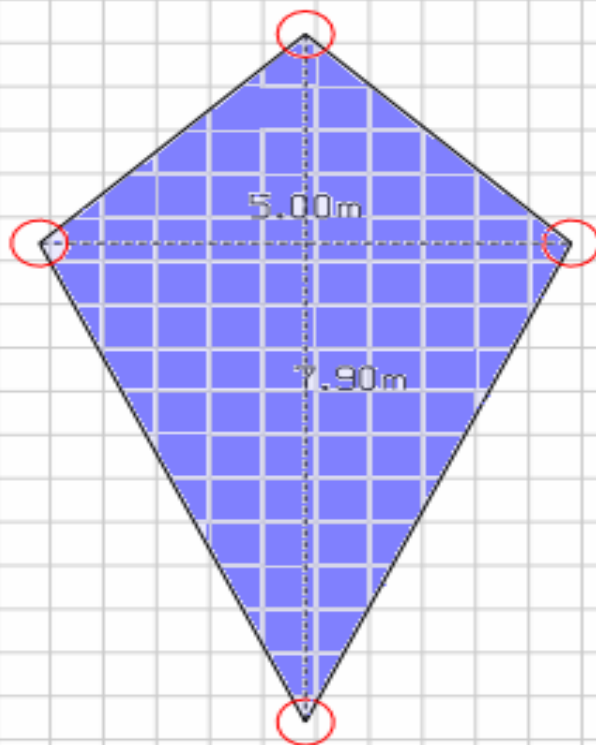


Crocodile Mathematics

Area of a kite

The area of a kite is half the product of its diagonals.

Drag any of the circled points to investigate



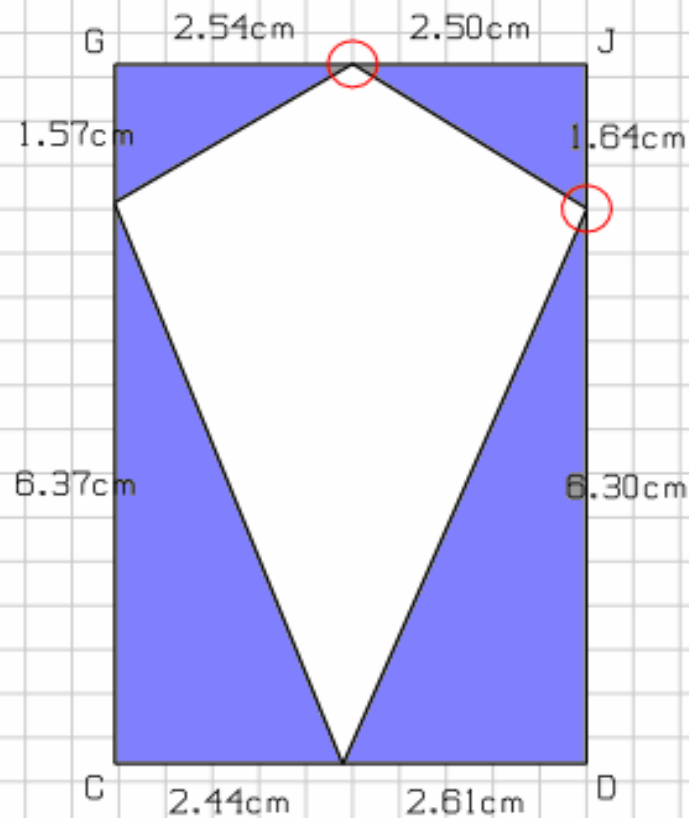
$$\begin{aligned}\text{Area of kite} &= \frac{1}{2} \times 5.00 \times 7.90 \\ &= 19.75 \text{ m}^2\end{aligned}$$

Crocodile Mathematics

Area of a Kite (2)

The area of a kite is equal to half the area of its surrounding rectangle.

Drag the circled points below to investigate



Area of kite = 20.05 cm²

Area of grey area = 20.05 cm²

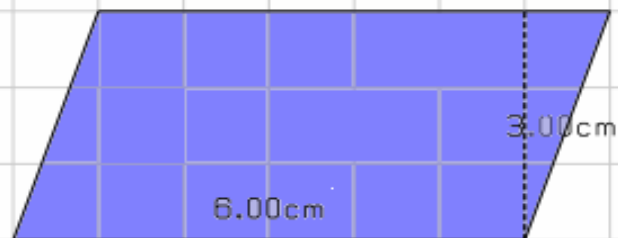
Crocodile Mathematics

Area of a parallelogram

Area of a parallelogram = base x height

You will notice that this is the same formula used to work out the area of a rectangle.

Drag the triangle at the right side of the parallelogram and move it across and join it to the left side of the parallelogram - the shape is now a rectangle!



Area of parallelogram = 6×3

$$= 18 \text{ cm}^2$$

Area of rectangle = 6×3

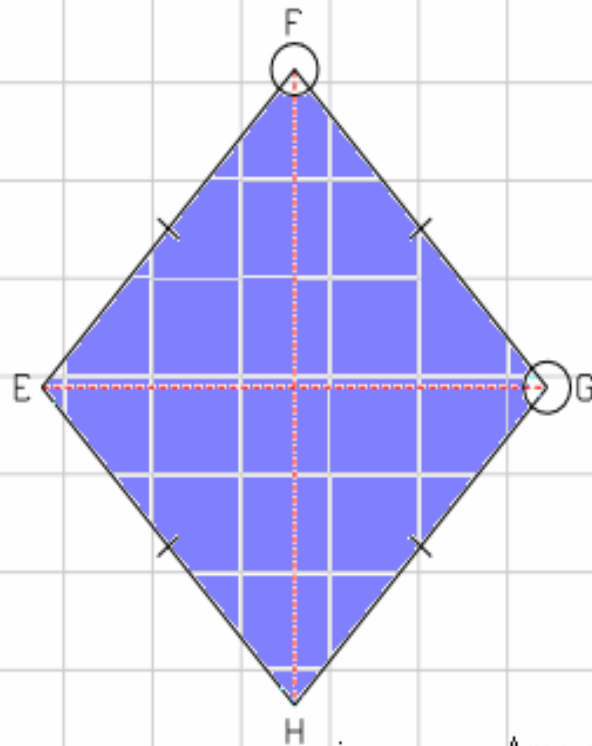
$$= 18 \text{ cm}^2$$

Crocodile Mathematics

Area of a Rhombus

The area of a rhombus is half the product of its diagonals.

Drag the circled points to investigate.



Line FH = 6.49 cm

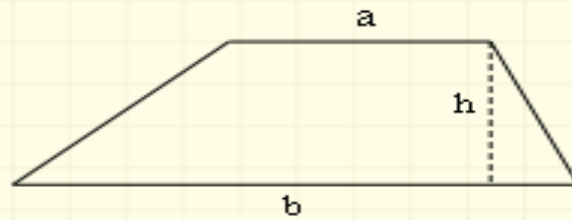
Line EG = 5.70 cm

$$\text{Area of EFGH} = \frac{1}{2} \times 6.49 \times 5.70$$

$$= 18.49 \text{ cm}^2$$

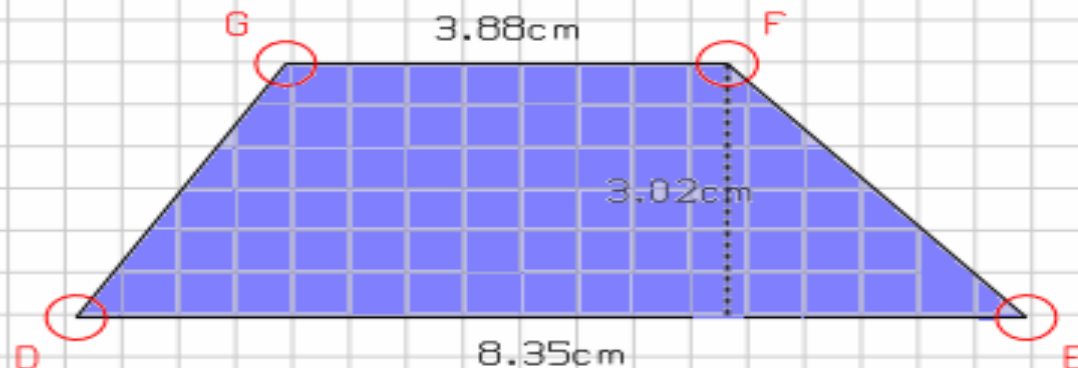
Crocodile Mathematics

Area of a Trapezium



$$\text{Area of trapezium} = \frac{1}{2} (a + b) h$$

Drag the circled points in the trapezium below to investigate



$$\begin{aligned} \text{Area DEFG} &= 0.50 \times (3.88 + 8.35) \times 3.02 \\ &= 18.45 \text{ cm}^2 \end{aligned}$$